EVALUATION OF CONTINGENCY ALLOCATION METHODS FOR

TRANSIT PROJECTS IN THE U.S. AND U.K.

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Abstract

In this paper, two probabilistic approaches for contingecy budget calculation developed and used in the

United States and United Kingdom are compared. In the first approach, the method used by the Federal

Transit Administration (FTA) of the U.S. Department of Transportation is reviewed. This approach is based

upon a range estimating concept. In the second approach, the method applied by the British Department for

Transport (DfT) is analyzed. The DfT suggests increasing project contingency in order to cope with the

optimism bias in infrastructure transportation projects. This approach relies on cumulative distribution

function (CDF), developed by considering historical projects in the same category. This paper evaluates

these two methods and makes a quantitative comparison of the results obtained by these methods. This is

accomplished by analyzing the cost performance data of a group of major transit projects in the U.S.,

applying the two methodologies, and comparing and analyzing the results. The problem areas of these

approaches are discussed and recommendations are made to optimize the use of these techniques. The paper

will be useful for owner agencies that are in charge of planning and executing large transit projects in the

face of cost uncertainty.

Keywords: Contingency, Budget, Risk, Top-down Model, Optimism Bias.

1

1. Introduction

Cost overrun has plagued transportation projects in various parts of the world for the past several decades (Flyvbjerg, 2002). Research has shown that this is due to many different reasons, including optimistic original estimates, lack of scope definition at the start of the project, increase in scope during the project development phase due to pressure from project stakeholders, errors in estimation, and lack of appropriate contingency budget (Booz Allen Hamilton, 2005). An owner agency usually adds an amount known as "contingency" to the estimated project cost to absorb the monetary impact of the risks and to prevent cost overrun. In the past few years, many agencies have resorted to the use of probabilistic means to quantify the uncertainties associated with project cost and allocate proper contingency budget.

In this paper, two probabilistic approaches for contingency allocation developed and used in the United States and United Kingdom for transit projects are illustrated and examined. In the first approach, the method used by the Federal Transit Administration (FTA) of the U.S. Department of Transportation is reviewed. FTA requires a formal risk assessment for all new transit projects. In this method, various project cost components are treated as random variables and are *ranged* according to predetermined values to explicitly model the variability of each major cost component. The sum of these cost components will be a distribution that represents the total cost. These sums are calculated with different assumptions regarding the correlations among cost components and are used to established budget contingencies. In the second approach, the British Department for Transport method that suggests increasing project contingency in order to cope with the *optimism bias* present in infrastructure transportation project cost estimates is examined. This is done by considering a cumulative distribution function of the amounts of overruns in previous projects and specifying a confidence limit for the project at hand for establishing a revised budget. The purpose of the paper is to illustrate the probabilistic approaches currently used in transportation industry. The author will not critically examine theoretical foundations of these approaches as that would require space beyond the scope of this paper.

2. Federal Transit Administration (Top-down) Model

2.1. Top-down Model Background

Federal Transit Administration (FTA) of the U.S. Department of Transportation (DOT) sponsors and provides technical support assistance to local transit authorities to carry out their transit projects. FTA, through a set of documented Project Guidance (PG) manuals and by procuring the services of Project Management Oversight Contractors (PMOCs), provides oversight assistance to transit authorities. Among the PGs, PG-40 "Risk Management Products and Procedures" (March 2007) is used for conducting risk analysis of all new transit projects. This probabilistic risk assessment, referred to as "Top-down model," is a "holistic view of all risks associated with the projects," rather than a listing of all risks in a risk register. FTA approach asserted that assessment of project risks considering discrete risk events could not capture the variability that is witnessed in current transit projects (Sillars and O'Connor, 2008). The PG's stance was that to focus on significant but few risk items instead of project risk as a whole may be masking risks that are unconsidered or individually small, but in total have a significant impact on the final cost.

2.2. Top-down Model Methodology

FTA classifies all costs of a new transit project into ten Standard Cost Categories (SCC): SCC-10 to SCC-100. Figure 1 shows all ten categories.

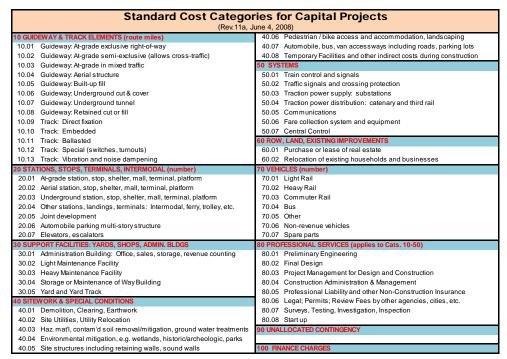


Figure 1: Standard Cost Categories (SCC), USDOT

Costs in SCC 90, Unallocated Contingency, and SCC 100, Financial Charges, are not considered in the Top-down procedure. The remaining categories should be carefully reviewed to identify all allocated contingencies. Then, these contingencies are removed from the estimate to arrive at the Base Cost Estimate (BCE) in each category (Sillars and O'Connor, 2008). Using Top-down model, the overall necessary contingency budget with respect to different confidence levels is determined. The approach assumes that each cost category follows a lognormal distribution that can be identified by estimating the 10th and 90th percentile values of each cost component. The BCE is usually considered to be the 10th percentile of the lognormal distribution. The 90th percentile of the distribution is estimated from Eq. (1):

90 × Percentile of the Distribution =
$$\beta$$
 × 10 × Percentile of the Distribution (1)

 β is dependent on the level of risk in project delivery stages and ranges from 1.0 to 2.5 and above. A β value of 1.0 means that there is no risk associated with the BCE. The more the project progresses, the smaller the value of β . Using the 10th and 90th percentile of each cost component, and using Lognormal Distribution equations, the mean and standard deviation of each cost component are calculated (Eqs. (2)-(7)). In these equations, μ and σ are parameters of the underlying normal distribution; \emptyset denotes the standard normal distribution and \emptyset^{-1} represents the inverse of cumulative function for the standard normal distribution; the mean and variance of the lognormal distribution are given in Eqs. (6) and (7).

$$x_a = Optimistic Estimate\% = Cost of 10^{th} Percentile in Each SCC$$
 (2)

$$x_h = Pesimistic Estimate\% = Cost of 90^{th} Percentile in Each SCC$$
 (3)

$$\mu = \frac{1}{2} \ln(x_a x_b) - \frac{\left[\phi^{-1}(a) + \phi^{-1}(b)\right]}{2} \sigma \tag{4}$$

$$\sigma = \ln\left(\frac{x_a}{x_b}\right) / [\emptyset^{-1}(b) - \emptyset^{-1}(a)]$$
(5)

$$Mean = e^{\mu + \sigma^2/2} \tag{6}$$

$$Variance = e^{2\mu + \sigma^2} (e^{\sigma^2} - 1)$$
 (7)

The sum of these cost components that represents the total cost is calculated using the Central Limit Theorem and assumes normality for the sum of lognormal components. To form the cumulative distribution, the model first assumes that all cost categories are completely correlated, r = 1.0, and then assumes that

there is no correlation, r = 0. This procedure produces two cumulative distributions for total cost. Note that the assumption of normality is not correct when components are fully correlated. Indeed, it can be proven that the total will follow a lognormal distribution. However, this is what the top-down approach assumes. A "First Order Approximation" distribution, which is the final product of the proposed top-down approach, is created by finding the one-third point of the total difference in variance between the two aforementioned distributions. This process is applied to project cost components, and several scenarios are run at the beginning of various project phases.

2.3. How to Assign β Values to Different SCCs at the Various Project Delivery Stages

Based on the historical data and lessons learned from previous transit projects, a set of recommended β values is suggested by PG-40. It is a risk analyst's responsibility to find the most appropriate β factors to assign to each SCC by considering the unique and specific characteristics of every project:

- 1. Requirement risks: those associated with the definition of basic project needs and transit system requirements to meet those needs ($\beta \ge 2.5$);
- 2. Design risks: those involved with the engineering design of the transit system (2.5> $\beta \ge 2.0$);
- 3. Market risks: those associated with the procurement of construction services and other system components (2.0> $\beta \ge 1.75$);
- 4. Construction risks: those associated with the actual construction of the systems (1.75> $\beta \ge 1.05$).

The guidelines provide specific β values to be applied to various Standard Cost Categories (SCC) for the transit project. The values of β may vary throughout project implementation at each key stage of project development. These recommendations will be used in the next section to assign the β 's at three different stages of the project completion.

2.4. Applying the Top-down Model to U.S. Data

The value of β will vary from project to project and depend on the level of project development. As the project design progresses, the values of β tend to decrease. However, one can estimate an average β for the average transit project in the United States. The objective here is to calculate the average range for U.S.

transit projects costs using the guidelines provided in PG-40. To this end, 51 transit projects in the U.S. (30 heavy rail and 21 light rail) for which actual costs were reported (Booz Allen Hamilton, 2003 and 2004) were identified. Using these cost data, the breakdown of costs for the average of these 51 transit projects were calculated for various cost categories. The result is illustrated in Figure 2.

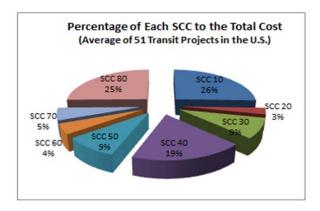


Figure 2: Percentage of Each Scc to the Total Cost

The β factors, using the FTA recommendations, are assigned for three different key phases of a project. These three phases are: Draft Environmental Impact Statement (DEIS), Preliminary Engineering (PE), and Final Design (FD). These phases are commonly used for transit project development in the U.S. and are roughly equivalent to Conceptual Design, Preliminary Engineering, and Final Design phases of project development. These values are given in Table 1. It can be seen that following this procedure, for example, at the PE stage, the average β value is 2.2. This means that the 90th percentile cost is more than twice as large as the 10th percentile cost.

Table 1: β Values Assigned to Each Cost Category at Three Key Phases of a Transit Project

scc	Average of 30 HRT Project	Average of 21 LRT Project	Average of 51 Transit Projects	% of Each SCC to Total Cost	Beta @DEIS	Beta @PE	Beta @FD
SCC 10	\$191,915,256	\$145,732,385	\$172,660,755	25.55%	2.50	2.25	2.00
SCC 20	\$20,763,234	\$16,594,973	\$19,427,829	2.88%	2.50	2.25	2.00
SCC 30	\$61,752,584	\$51,401,222	\$58,640,064	8.68%	2.50	2.25	2.00
SCC 40	\$179,590,760	\$42,208,831	\$125,482,165	18.57%	2.77	2.50	2.22
SCC 50	\$62,638,602	\$56,277,600	\$61,219,753	9.06%	2.50	2.25	2.00
SCC 60	\$26,399,332	\$35,113,473	\$30,587,258	4.53%	4.37	3.93	3.50
SCC 70	\$38,409,454	\$32,770,106	\$36,809,117	5.45%	1.87	1.68	1.50
SCC 80	\$198,569,935	\$123,061,639	\$170,827,849	25.28%	1.87	1.68	1.50
		·	Total		Weighted Average of Beta		
			\$675,654,790	100%	2.44	2.20	1.96

For the average transit project, the 10th percentile is assumed to be the value of BCE, and the 90th percentile is calculated using Eq. (1). Values of mean and standard deviation in each category are calculated using Eqs. (2)-(7).

Then, all SCCs are summed to generate Total Cost, assuming independence and perfect correlation among cost BCEs. In both cases, following the FTA guide, the mean of the total cost is assumed to be a Normal distribution. Using the correlation coefficient and variance definitions to find the standard deviation of the total cost, it is known that:

- when all cost components are independent, the standard deviation of the total cost is the square root of the sum of all cost component variances; and
- 2. when all cost components are fully correlated, the standard deviation of the total cost is simply the sum of all cost component standard deviations.

The result is given in Table 2.

Table 2: 10th Percentile, 90th Percentile, Mean and Std. Deviation of Each Cost Category

	10th Percentile	DEIS Stage			PE Stage			FD Stage		
scc		90th Percentile	Mean	Std. Dev.	90th Percentile	Mean	Std. Dev.	90th Percentile	Mean	Std. Dev.
SCC 10	25.6%	63.9%	43.07%	15.90%	57.5%	40.30%	13.08%	51.1%	37.49%	10.33%
SCC 20	2.9%	7.2%	4.85%	1.79%	6.5%	4.53%	1.47%	5.8%	4.22%	1.16%
SCC 30	8.7%	21.7%	14.63%	5.40%	19.5%	13.69%	4.44%	17.4%	12.73%	3.51%
SCC 40	18.6%	51.4%	33.45%	13.84%	46.4%	31.30%	11.56%	41.2%	29.04%	9.26%
SCC 50	9.1%	22.7%	15.27%	5.64%	20.4%	14.29%	4.64%	18.1%	13.29%	3.66%
SCC 60	4.5%	19.8%	11.17%	7.00%	17.8%	10.35%	5.94%	15.8%	9.54%	4.96%
SCC 70	5.4%	10.2%	7.68%	1.90%	9.2%	7.21%	1.47%	8.2%	6.76%	1.08%
SCC 80	25.3%	47.3%	35.62%	8.83%	42.5%	33.45%	6.84%	37.9%	31.36%	4.99%
Total (Correlated)		·	165.73%	60.30%		155.12%	49.44%		144.43%	38.94%
Total (Independent)			165.73%	25.28%		155.12%	20.79%		144.43%	16.43%

Following the Top-down model process, cumulative normal distributions for each phase, assumed completely correlated and independent, are formed, and the first order approximation curves are generated. This procedure is done employing an Excel spread sheet. Having the mean and standard deviation of the total cost, the cumulative distribution is produced using the NORMINV command of Excel for a probability range of 0-100%. Figure 3 shows the first order approximation curves for three different phases.

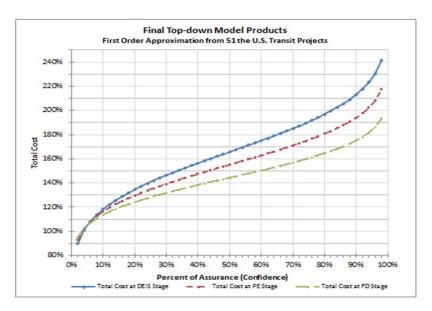


Figure 3: Final Top-down Model Curves (Total Required Budget) at Three Different Phases of a Transit Project

Using Figure 3, if an agency wants to establish a project budget at the "Final Design" phase of a project with 85% confidence that the budget is sufficient, it should allocate a budget equal to 1.69 of the initial cost estimate (Total BCEs). It should be noted that since, in a transit project, a contingency budget is added to the Base Cost Estimate (BCE), and this contingency varies according to the project phase, the amount of uplift (i.e. increase in the original budget) compared to the budgeted estimate should be smaller. "Uplift" is the term used to show the amount that the original estimate needs to be increased to arrive at the project budget for a given level of certainty (e.g. confidence level of 50% or 90%) with respect to budget adequacy (Flyvbjerg, 2006). For example, a typical contingency added to the BCE at the Final Design phase is about 10%. This means that the estimated budget should be increased by 1.69/1.10 = 1.54 (or 54%). Since transit projects usually are costly, it means that the agency must provide and block a huge amount of money to ensure a sufficient budget. Figure 4 is a modified version of Figure 3. The X axis is converted to the "Acceptable Chance of Cost Overrun", 100% - Percent of Assurance (Confidence), and the Y axis to "Required Uplift" (or the amount needed to be added to the base cost), Total Cost - 100%. This modification was done to make Figure 4 similar to the final product of the British Department for Transport (Optimism Bias) Model. The outcome of this analysis with the British approach will be compared later in this paper. As an example, increasing the base budget by 69% (at the Final Design phase), will mean that there is a 15% chance that the budget will not be sufficient, *i.e.*, there will be a cost overrun.

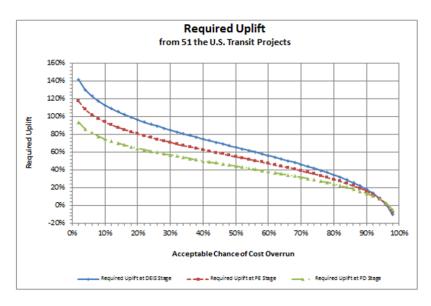


Figure 4: Converted Curves of the Top-down Model to Show the Required Uplift

3. The British Department for Transport (Optimism Bias) Model

3.1. Optimism Bias Model Background

The second approach examined for this research is the British Department for Transport (DfT) approach in dealing with optimism bias in capital project cost estimates. This method establishes an increase (uplift) in the original project budget estimate based upon different project categories (road, rail, etc.) and the level of risk that the DfT is willing to accept regarding cost overrun. According to Flyvbjerg *et al* (2002, 2005, 2006), psychological (optimism bias) and political explanations (strategic misrepresenting due to political and organizational pressure) are responsible for much of the inaccuracy in transportation cost forecasting. Flyvbjerg *et al* (2005) recommended a new forecasting method called "reference class forecasting" to reduce inaccuracy and bias. Reference class forecasting method, which has proven more accurate than conventional forecasting, is based on theories of decision-making under uncertainty. "Reference class forecasting does not try to forecast the specific uncertain events that will affect the particular project, but instead places the project in statistical distribution of outcomes from the class of reference projects." (Flyvbjerg 2006). To implement the reference class forecasting on an individual project, three steps are required: (1) Finding a relevant reference class of past projects; (2) Establishing a probability distribution for the selected reference class; and (3) In order to find the most likely outcome for the project under consideration, making a

comparison between the project under consideration and the reference class distribution (Flyvbjerg *et al*, 2005).

According to Supplementary Green Book (2003): "There is a demonstrated, systematic tendency for project appraisers to be overly optimistic. To redress this tendency, appraisers should make explicit, empirically based adjustments to the estimates of a project's costs, benefits, and duration... It is recommended that these adjustments be based on data from past projects or similar projects elsewhere." To this end, in 2004, the British Department for Transport and HM Treasury published a guide, "Procedures for dealing with Optimism Bias in Transport Planning," based on the work conducted by Flyvbjerg and COWI (The British DfT, 2004). It establishes a guide for selected reference classes of transport infrastructure projects to prevent cost overrun. This approach is hereafter called the "Optimism Bias Model" method in this paper.

3.2. The Optimism Bias Model Methodology

In the DfT guide, transportation projects have been divided into a number of distinct groups. These groups include road, rail, fixed links, buildings, and IT projects and have been selected in order to have statistically similar risk of cost overrun based on the study of an international database of 258 transportation projects. In this paper, the focus is only on rail projects, as the analyzed transit projects for the US case were almost exclusively rail projects.

In the DfT guide, cost overrun is defined as the difference between the actual cost (final cost) and the estimated cost, which is the forecasted cost at the time of approval of/decision to build a project, in percentage of estimated cost. Where the approval point is not clear in the project planning process, the closest available estimate is used. For each category, the probability distribution for cost overrun as the share of projects with a given maximum cost overrun was created. Having established the empirical cumulative distribution, uplifts are set up as a function of the level of risk that the DfT is willing to accept regarding cost overrun. If the DfT wants to accept a higher risk, then a lower uplift is required. The readers are referred to the British DfT (2004) and Flyvbjerg (2006) for a thorough description of the Optimism Bias methodology.

3.3. Applying the Optimism Bias Model to U.S. Data

To generate a reference class, 22 rail projects across the U.S. were selected. To reach the objective of this paper, the Optimism Bias Model approach is first applied to these projects. Then the results are compared with the results of applying the USDOT approach to the same data. These projects were part of a study conducted by Booz Allen Hamilton (2005). As part of this research effort, cost overruns for 22 major rail projects were calculated by considering estimated budgets at various stages of these projects. For each project, the cost overrun/underrun was calculated at the DEIS, PE, and FD stages by comparing these estimates with the actual cost of projects. Although, DfT calculates the cost overrun relative to the estimate at the point of approval of/decision to build, in order to compare FTA and DfT models, cost overrun has been calculated at the DEIS, PE, and FD stages. PE can be considered equivalent to the British agencies' preparation of their initial budgets. In this way, these two models can be compared. It should be noted that the main criteria in selecting these 22 projects for inclusion in the original study was the availability of data. In other words, the author was not trying to identify and select projects that were notorious for cost overrun or delay.

In order to find the probability distribution for each stage, the cost overruns/underruns of 22 projects were sorted in ascending order. Then, for each cost overrun/underrun, the correspondent probability was calculated by dividing the number of projects having the cost overrun less than that by 22. Figure 5 depicts the probability distributions for the DEIS, PE, and FD stages. For instance, Figure 5 shows that at the DEIS stage, 60% of projects have the maximum cost overrun of 23%. Then the required uplift curve is calculated (Figure 6).

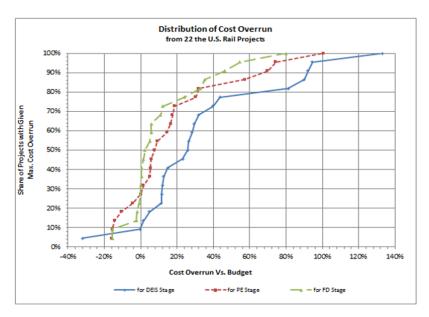


Figure 5: Probability Distribution of Cost Overrun at Three Different Stages of a Project

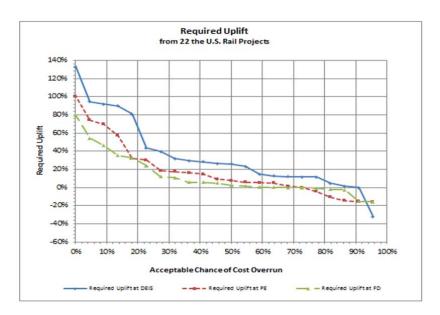


Figure 6: Required Uplifts at Three Different Stages of a Project

Figure 6 illustrates that, based on the selected U.S. projects, if a transit agency decides to apply the method suggested by the DfT and to accept a 10% chance of cost overrun for its project, the required uplift is 91.61% at the DEIS phase, 67.36% at the PE phase, and 44.01% at the FD phase. It demonstrates that the more a project progresses, the less uplift is required, due to the decreasing level of uncertainty.

4. Comparison of Top-down and Optimism Bias Models

In previous sections, two different probabilistic approaches to a group of transit projects in the U.S. were applied. Although the Optimism Bias approach used in the U.K. only considers the cost estimate at the approval of/decision to build stage of a project when calculating cost overrun, in order to evaluate β values of the Top-down model used in the U.S., in this paper, cost overrun was calculated at the three DEIS, PE, and FD phases. Comparing Figure 4 and Figure 6 shows that required the uplift for 50% confidence at the PE stage is 55.12% with the Top-down model and 7.70% with the Optimism Bias approach. Table 3 lists the required uplift for 50% confidence at the three stages of the project for the two approaches.

Table 3: Required Uplift with 50% Acceptable Chance of Cost Overrun with Two Approaches

Model	Required Uplift with 50% Confidence				
Model	DEIS	PE	FD		
Top-down approach	65.73%	55.12%	44.43%		
Optimism Bias approach	25.96%	7.70%	2.37%		

Comparing these results shows that the Top-down approach established a much larger budget for the project. Establishing too conservative a budget is not necessarily desirable because, by tying up excessive funds for some projects, other candidate projects will be deprived of necessary funds. In the Top-down Methodology, remember that β is defined as the ratio between the 90th percentile and 10th percentile of the cumulative cost distribution. Using the data in Figure 5, equivalent β values for the Optimistic Bias approach can be constructed by calculating the ratio between the 10th and 90th percentile points. In Table 4, the calculated β values are compared with weighted average of β values recommended by the Top-down model (computed in Table 1).

Table 4: Comparison of the β Values in Two Approaches

	O	otimism Bias	Top-down		
Key Stages	10 th Percentile	90 th Percentile	β	Weighted Average β	
DEIS	1.001	1.916	1.91	2.44	
PE	0.847	1.674	1.97	2.20	
FD	0.872	1.440	1.65	1.96	

Reviewing Table 4 shows that β values from the Optimism Bias approach, where the data is determined from historical data, are significantly smaller than the β values recommended by the Top-down approach. Looking at β s for the Optimism Bias approach illustrates that the values of β at the PE stage are greater than

at the DEIS stage, when it should normally be smaller. This is due to the greater number of projects that have had cost underrun in the DEIS stage, compared to the PE stage, due to scope reduction.

5. Conclusion

Owners usually need to have an accurate early cost estimate for their projects in order to provide a sufficient budget. Since contingency is part of a project budget, this reveals the importance of estimating it as accurately as possible in the early stage of project life. Optimism Bias and Top-down approaches are suggested (and used) to establish contingency budgets for transit projects in the U.S. and the U.K. Both approaches have positive and negative aspects. First, the Top-down model selects large values of β for ranging cost components in order to prevent cost overrun, which results in establishing a budget far larger than historical actual costs. The Optimism Bias approach is based on historical data, but does not consider the unique features and characteristics of individual projects. It gives an estimate of the actual cost based on a set of peer projects without considering the location and special conditions of each projects. The positive aspect of both approaches is the explicit consideration of uncertainty in cost estimating and budgeting. Also, both approaches are relatively simple and quick to apply, as they do not rely on developing risk registers. Developing a risk register through risk workshops, especially for large projects, can be a time consuming task and involves large expenses. Moreover, based on the analysis performed in this research, it seems that applying the Optimism Bias approach, which considers the performance of similar past projects, led to the allocation of a smaller contingency budget than Top-down approach. The author's suggestion is to refine these approaches and come up with a probabilistic method that considers the unique characteristics of each project without tying up huge capital in order to prevent potential cost overruns. Moreover, it should be noted that the schedule and the cost of construction projects are somehow related. Therefore, the use of models in which cost and schedule risks are integrated should be considered.

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